

B.Sc. Semester - 4 (NEP-2020) Examination

March/April-2025

MATH: Advanced Calculus -2 (Major-9)

Time: 2:00 Hours

Marks: 50

Instructions:

1. All questions are compulsory.
2. Figures to the right indicate marks.

- Que-1 Answer any two. (10)
1. Define: Lagrange's partial differential equation and derive its auxiliary equation.
 2. Form a partial differential equation by elimination of arbitrary function method:
 $\varphi(x^2 + y^2 + z^2; z^2 - 2xy) = 0$.
 3. Using Charpit's method, solve: $(p^2 + q^2)y = qz$
- Que-2 Answer any two. (10)
1. Derive Monge's equations for non-linear equation of the second order for
 $R_r + S_s + T_t = V$
 2. Using Monge's method, solve: $r - t\cos^2 x + p\tan x = 0$.
 3. Solve: $(D^2 + DD' - 6D'^2)z = x^2 \cos(x + y)$.
- Que-3 Answer any two. (10)
1. Define: Laplace transform. Prove that:

$$L(t^n) = \frac{\Gamma(n+1)}{s^{n+1}}; s > 0, n > -1.$$

$$= \frac{n!}{s^{n+1}}; n = 0, 1, 2, 3, \dots$$
 2. Find Laplace transform of (i) $\sin 2t \cos 3t$ (ii) $\cosh^3 2t$.
 3. If $L\{f(t)\} = \bar{f}(s)$ then prove that: $L\{e^{at}f(t)\} = \bar{f}(s-a)$. Using it find: $\{e^{-3t} \sin^2 t\}$.
- Que-4 Answer any two. (10)
1. State and prove convolution theorem for inverse Laplace transforms.
 2. Find the inverse Laplace transform of (i) $\frac{3s+5}{(s+1)^4}$ (ii) $\frac{s+7}{s^2+2s+2}$.
 3. Solve: $y'' + y = t, y(\pi) = 0, y'(0) = 1$.
- Que-5 Answer any two. (10)
1. Solve: $(D^3 - 3D^2D')z = x^2y$.
 2. Solve: $xp + yq = 1$.
 3. Define: Inverse Laplace transform. Find the inverse Laplace transform of $\frac{1}{s^3(s^2+a^2)}$.
